

$$L := 290 \text{ m} \quad d := 16 \text{ m} \quad B := 47.5 \text{ m} \quad C_b := 0.805 \quad V := 15 \text{ knot}$$

$$\rho := 1.025 \frac{\text{tonne}}{\text{m}^3} \quad \Delta := C_b \cdot L \cdot B \cdot d \cdot \rho \quad \Delta = (1.81858 \cdot 10^5) \text{ tonne}$$

$$x_t := \frac{-L}{2} \quad x_t = -145 \text{ m} \quad x'_t := \frac{x_t}{L} \quad x'_t = -0.5$$

$$T := 10 \text{ kN} \quad T' := \frac{T}{\frac{1}{2} \cdot \rho \cdot L^2 \cdot V^2} \quad T' = 3.896 \cdot 10^{-6}$$

Clarke coefficients (linear velocity and acceleration)

$$Y'_{vdot} := -\pi \cdot \left(\frac{d}{L}\right)^2 \cdot \left(1 + 0.16 \cdot C_b \cdot \frac{B}{d} - 5.1 \cdot \left(\frac{B}{L}\right)^2\right) \quad Y'_{vdot} = -0.012$$

$$Y'_{rdot} := -\pi \cdot \left(\frac{d}{L}\right)^2 \cdot \left(0.67 \cdot \frac{B}{L} - 0.0033 \cdot \left(\frac{B}{d}\right)^2\right) \quad Y'_{rdot} = -7.713 \cdot 10^{-4}$$

$$N'_{vdot} := -\pi \cdot \left(\frac{d}{L}\right)^2 \cdot \left(1.1 \cdot \frac{B}{L} - 0.041 \cdot \frac{B}{d}\right) \quad N'_{vdot} = -5.59 \cdot 10^{-4}$$

$$N'_{rdot} := -\pi \cdot \left(\frac{d}{L}\right)^2 \cdot \left(\frac{1}{12} + 0.017 \cdot C_b \cdot \frac{B}{d} - 0.33 \cdot \frac{B}{L}\right) \quad N'_{rdot} = -6.685 \cdot 10^{-4}$$

$$Y'_v := -\pi \cdot \left(\frac{d}{L}\right)^2 \cdot \left(1 + 0.40 \cdot C_b \cdot \frac{B}{d}\right) \quad Y'_v = -0.019$$

$$Y'_r := -\pi \cdot \left(\frac{d}{L}\right)^2 \cdot \left(-0.5 + 2.2 \cdot \frac{B}{L} - 0.08 \cdot \frac{B}{d}\right) \quad Y'_r = 0.004$$

$$N'_v := -\pi \cdot \left(\frac{d}{L}\right)^2 \cdot \left(0.5 + 2.4 \cdot \frac{d}{L}\right) \quad N'_v = -0.006$$

$$N'_r := -\pi \cdot \left(\frac{d}{L}\right)^2 \cdot \left(0.25 + 0.039 \cdot \frac{B}{d} - 0.56 \cdot \frac{B}{L}\right) \quad N'_r = -0.003$$

$$Y'_\delta := 3186 \cdot 10^{-6} \quad N'_\delta := -1402 \cdot 10^{-6} \quad m' := 14622 \cdot 10^{-6} \quad mxG' := 365 \cdot 10^{-6} \quad I'_{zz} := 766 \cdot 10^{-6}$$

$$M' := \begin{bmatrix} -Y'_{v\dot{d}ot} + m' & -Y'_{r\dot{d}ot} + mxG' \\ -N'_{v\dot{d}ot} + mxG' & -N'_{r\dot{d}ot} + I'_{zz} \end{bmatrix}$$

$$M' = \begin{bmatrix} 0.027 & 0.001 \\ 9.24 \cdot 10^{-4} & 0.001 \end{bmatrix}$$

$$D' := \begin{bmatrix} -Y'_v & -Y'_r + m' \\ -N'_v & -N'_r + mxG' \end{bmatrix}$$

$$D' = \begin{bmatrix} 0.019 & 0.011 \\ 0.006 & 0.003 \end{bmatrix}$$

$$R' := \begin{bmatrix} Y'_\delta \\ N'_\delta \end{bmatrix}$$

$$R' = \begin{bmatrix} 0.003 \\ -0.001 \end{bmatrix}$$

$$Thrust := \begin{bmatrix} T' \\ T' \cdot x'_t \end{bmatrix}$$

$$Thrust = \begin{bmatrix} 3.896 \cdot 10^{-6} \\ -1.948 \cdot 10^{-6} \end{bmatrix}$$

You hadn't defined  $\delta$ , so I set an arbitrary value here:  $\delta := 1$

Easier to solve if you separate  $x1'$  and  $x2'$

$$soln(x1, x2) := M' \cdot \begin{bmatrix} x1p \\ x2p \end{bmatrix} + D' \cdot \begin{bmatrix} x1 \\ x2 \end{bmatrix} = R' \cdot \delta + Thrust \xrightarrow{\text{solve}, x1p, x2p} \begin{bmatrix} 0.000055794282942704887032 \cdot m \\ \text{knot}^2 \cdot \text{tonne} \end{bmatrix}$$

Constants/Values

$$\frac{d}{dt} x1(t) = soln(x1(t), x2(t))_{0,0} \quad x1(0) = 0$$

$$\frac{d}{dt} x2(t) = soln(x1(t), x2(t))_{0,1} \quad x2(0) = 0$$

Solver

$$\begin{bmatrix} v \\ r \end{bmatrix} := \text{odesolve} \left( \begin{bmatrix} x1(t) \\ x2(t) \end{bmatrix}, 30 \right)$$

