

Ex.S6 Response of electric circuit when impulse response and input signal are shown as follows. Sinusoidal waves input. $R=1\Omega, L=1\text{ H}$ (Series connection)

$$R:=1 \quad L:=1 \quad Z(s):=R+s\cdot L \quad h(t):=e^{-t} \quad \text{impulse response}$$

$$h(t):=e^{-t} \quad H(s):=\frac{1}{s+1} \quad R:=1 \quad \omega:=1 \quad L:=1$$

$$H(\omega):=\frac{1}{1+\omega\cdot 1i} \quad H_0(\omega):=\sqrt{\text{Re}(H(\omega))^2 + \text{Im}(H(\omega))^2} \quad \phi(\omega):=\arg(H(\omega))$$

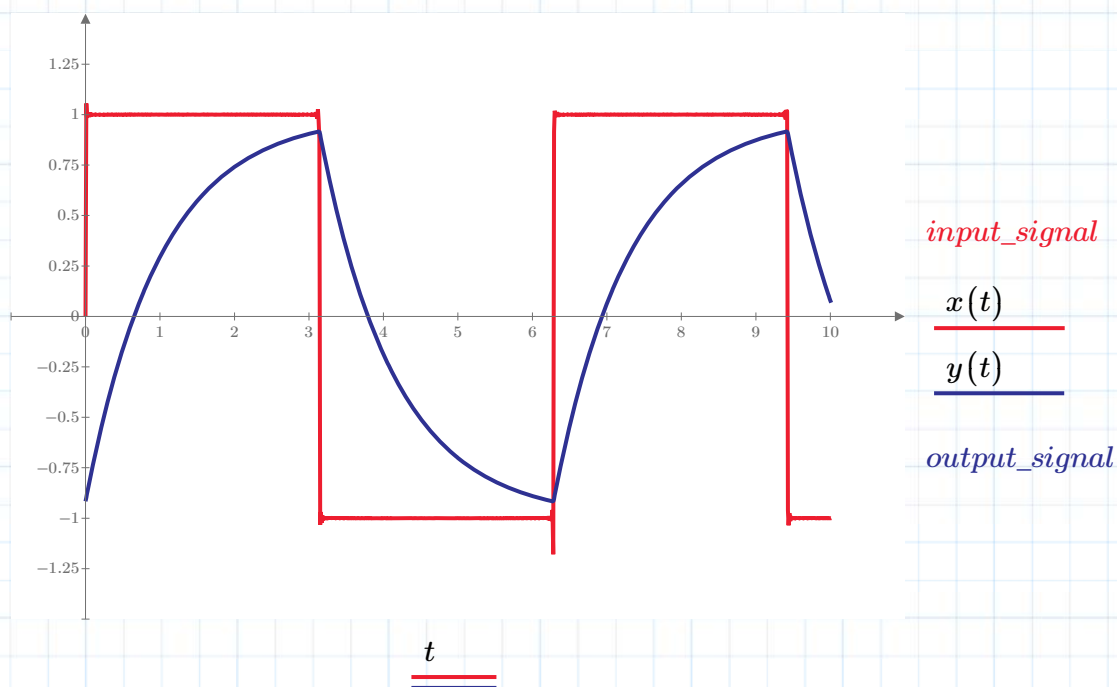
$$m:=500$$

$$n:=1,2\dots m \quad H_n := \frac{1}{1+(2n-1)\cdot 1i} \quad H_{0_n} := \sqrt{\text{Re}(H_n)^2 + \text{Im}(H_n)^2} \quad \phi_n := \arg(H_n)$$

$$t:=0,0.01\dots 10.1$$

$$x(t) := \sum_{n=1}^m \left(\frac{4}{\pi} \frac{1}{(2\cdot n-1)} \cdot \sin((2n-1)\cdot t) \right) \quad \text{input_signal}$$

$$y(t) := \sum_{n=1}^m \left(H_{0_n} \cdot \frac{4}{\pi} \cdot \frac{1}{(2\cdot n-1)} \cdot \sin((2n-1)\cdot t + \phi_n) \right) \quad \text{output_signal}$$



$$y(0) = -0.917$$

$$y(\pi) = 0.917$$

$$(1+A) \cdot e^{-\pi} - 1 = -A \xrightarrow{\text{solve, A}} \frac{2}{e^{-\pi} + 1} - 1 = 0.917$$

$$1.917 \cdot e^{-\pi} - 1 = -0.917$$