

## Valery's Rocket

$m_{PL} := 0.8 \cdot \text{tonne}$  Load mass  $m_o := 0.45 \cdot \text{tonne}$  Empty rocket mass

$b := 0.1 \cdot \frac{\text{kg}}{\text{s}}$  Shape Factor  $m_f := 9 \cdot \text{tonne}$  Fuel mass

$m_c(t) := 1 \cdot t \cdot \frac{\text{tonne}}{\text{s}}$  Fuel consumption  $u(t) := 2 \cdot \frac{\text{km}}{\text{s}}$  Propellant speed

$t_{end} := \left\| \begin{array}{l} t_{end} \leftarrow 10 \cdot \text{s} \\ \text{root}(m_f - m_c(t_{end}), t_{end}) \end{array} \right\|$   $t_{end} = 9 \text{ s}$  Time for empty the fuel

$m(t) := m_{PL} + m_o + m_f - m_c(t)$  Mass of the rocket as time function

$R := 6371 \cdot \text{km}$  Medium earth radius  $g(y) := g \cdot \left( \frac{R}{R+y} \right)^2$  Acc due gravity, as function of altitude

More accurate, accounting the latitude  $\varphi := 53 \cdot \text{deg}$

$g(y) := 1.002691423 \cdot \left( 1 + 0.0053024 \cdot \sin(\varphi)^2 - 0.0000058 \cdot \sin(2 \varphi)^2 \right) \cdot g(y)$

Newton Law  $F = \frac{d}{dt} p = \frac{d}{dt} \left( m \cdot \frac{d}{dt} y \right) = \frac{d}{dt} m \cdot \frac{d}{dt} y + m \cdot \frac{d^2}{dt^2} y$

Forces balance  $F = -m \cdot g - f_r$  with  $f_r = -b \cdot \frac{d}{dt} y$

**Solve Block**  $y(0 \cdot \text{s}) = 0 \cdot \text{m}$   $y'(0 \cdot \text{s}) = 0 \cdot \frac{\text{m}}{\text{s}}$

$-m(t) \cdot g(y(t)) - b \cdot \frac{d}{dt} y(t) = u(t) \cdot \frac{d}{dt} m(t) + m(t) \cdot \frac{d^2}{dt^2} y(t)$

**Solver**  $y := \text{Odesolve}(y(t), t_{end})$

Avoid the bound  $t_1 := t_{end} - 0.01 \cdot \text{s}$  y and y' plots  $tt := 0 \cdot \text{s}, 0.01 \cdot \text{s} .. t_1$

$y(t_1) = 12.298 \text{ km}$   $\frac{d}{dt} y(t_1) = 4.104 \frac{\text{km}}{\text{s}}$

Values from

$9000 \cdot 0.05 =$

mc' and u control sys

$g(300 \cdot \text{m})$

$g(300 \cdot \text{m})$

