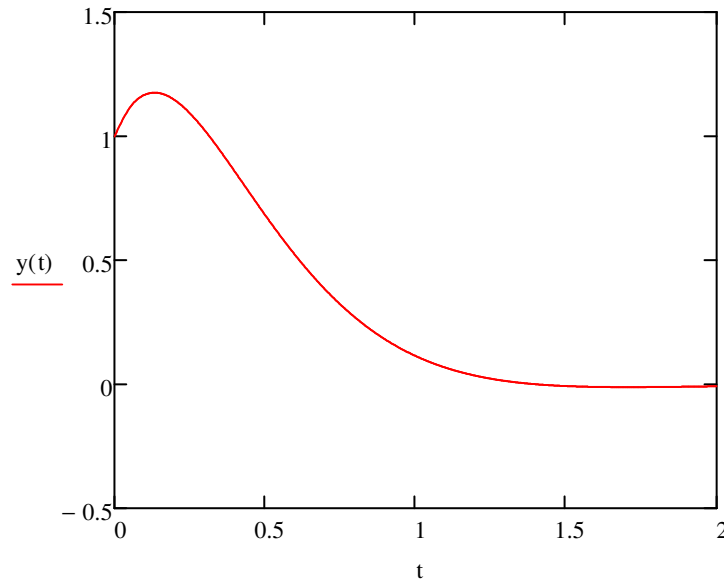


Given

$$y''(t) + 6 \cdot y'(t) + 13 y(t) = 0$$

$$y'(0) = 3 \quad y(0) = 1$$

`y := Odesolve(t, 50)`



You can get an analytical solution with the help of Mathcad's symbolic Laplace transform here, as follows:

### Step 1

$$\frac{d^2}{dt^2} Y(t) + 6 \cdot \frac{d}{dt} Y(t) + 13 \cdot Y(t) \text{ laplace} \rightarrow 6 \cdot s \cdot \text{laplace}(Y(t), t, s) - \left. \begin{array}{l} x0 \leftarrow 0 \\ \frac{d}{dx0} Y(x0) \end{array} \right| - 6 \cdot Y(0) + s^2 \cdot \text{lap}$$

### Step 2

Rewrite the RHS of the above using, say L, for  $\text{laplace}(Y(t), t, s)$  and noting that  $\left. \begin{array}{l} x0 \leftarrow 0 \\ \frac{d}{dx0} Y(x0) \end{array} \right|$  is just  $y'(0)$  ((unfortunately this has to be done by hand (at

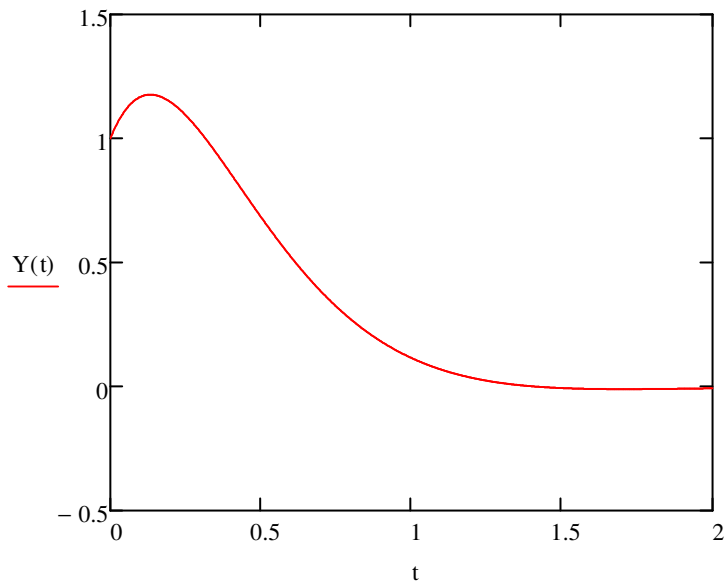
least, I can't find a way of getting Mathcad to do it automatically), set the result equal to zero, solve using symbolic "solve", and assign the result to function L(s), say.

$$\underline{\underline{L(s)}} := 6 \cdot s \cdot L - 3 - 6 + s^2 \cdot L - s + 13 \cdot L = 0 \text{ solve, } L \rightarrow \frac{s + 9}{s^2 + 6 \cdot s + 13}$$

**Step 3** Inverse laplace L(s) using symbolic "invlaplace" and assign to Y(t)

$$Y(t) := L(s) \text{ invlaplace} \rightarrow e^{-3 \cdot t} \cdot (\cos(2 \cdot t) + 3 \cdot \sin(2 \cdot t))$$

**Step 4** Plot Y(t) (compare with numerical y(t) above)  
(You should also differentiate Y(t) as necessary to see that you recover your original ODE)



$$\text{lace}(Y(t), t, s) - s \cdot Y(0) + 13 \cdot \text{laplace}(Y(t), t, s)$$