

Cable length: $L_0 := 15 \cdot \text{m}$

Sections: $N_S := 20$

$i := 0.. N_S - 2$

Min. x: $a := 0 \cdot \text{m}$

Max. x: $b := 10 \cdot \text{m}$

$y_a := 7 \cdot \text{m}$

$y_b := 10 \cdot \text{m}$

Function for sections:

Abschnitte(a, b, x, y) :=

$$\left\{ \begin{array}{l} \Delta s_0 \leftarrow \sqrt{(x_0 - a)^2 + (y_0 - y_a)^2} - \frac{L_0}{N_S} \\ \text{for } i \in 1.. N_S - 2 \\ \Delta s_i \leftarrow \sqrt{(x_i - x_{i-1})^2 + (y_i - y_{i-1})^2} - \frac{L_0}{N_S} \\ \Delta s_{N_S-1} \leftarrow \sqrt{(b - x_{N_S-2})^2 + (y_b - y_{N_S-2})^2} - \frac{L_0}{N_S} \\ \Delta s \end{array} \right.$$

Potential Energy:

$m_0 := 1 \cdot \text{kg}$

$$E_{\text{pot}}(x, y) := m_0 \cdot g \cdot \left(y_a + \sum_{i=0}^{N_S-2} y_i + y_b \right)$$

Initial values:

$$x_i := a + (i + 1) \cdot \frac{b - a}{N_S}$$

$$y_i := y_a + (i + 1) \cdot \frac{y_b - y_a}{N_S} - \frac{(x_i - a) \cdot (b - x_i)}{10 \cdot \text{m}}$$

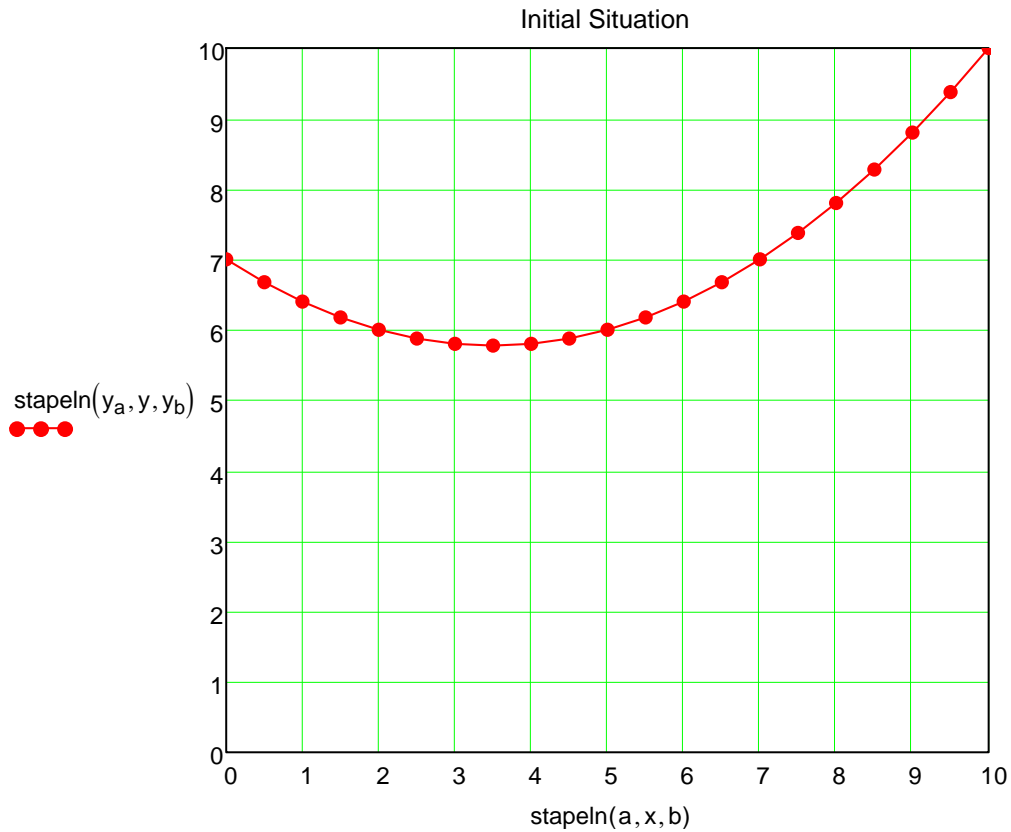
Abschnitte(a, b, x, y) =

	0
0	-0.154
1	-0.179
2	-0.202
3	-0.22
4	-0.235
5	-0.244
6	-0.249
7	-0.249
8	-0.244
9	-0.235
10	...

·m

$$\frac{\sqrt{(b - a)^2 + (y_b - y_a)^2}}{N_S} - \frac{L_0}{N_S} = -0.228 \cdot \text{m}$$

$$E_{\text{pot}}(x, y) = 1.424 \times 10^3 \cdot \text{J}$$



Minimize for cable:

Vorgabe

Abschnitte(a, b, x, y) = 0

$\begin{pmatrix} x \\ y \end{pmatrix} := \text{Minimieren}(E_{\text{pot}}, x, y)$

ERR = 3.464×10^{-13}

TOL = 1×10^{-8}

CTOL = 1×10^{-9}

Abschnitte(a, b, x, y) =

	0
0	0
1	0
2	0
3	$2.776 \cdot 10^{-15}$
4	$2.72 \cdot 10^{-14}$
5	$-1.155 \cdot 10^{-14}$
6	0
7	0
8	$-2.331 \cdot 10^{-13}$
9	$-2.381 \cdot 10^{-13}$
10	...

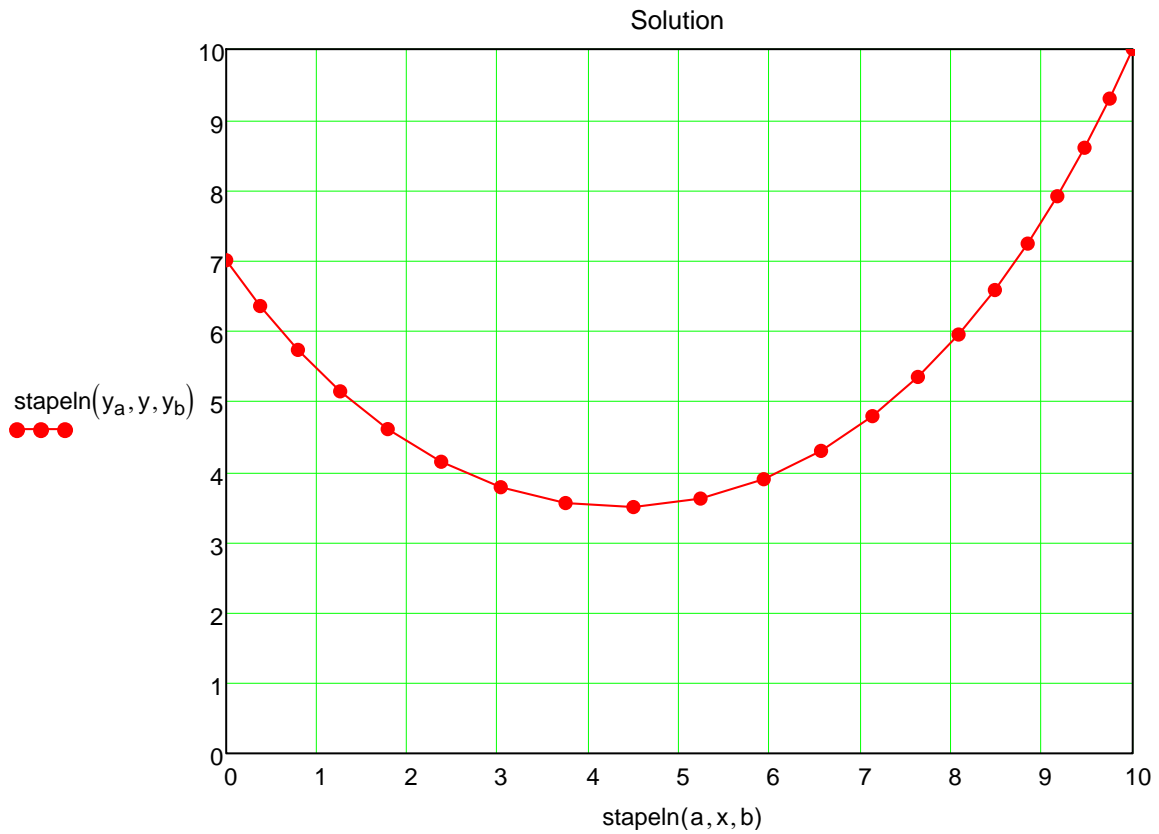
·m

$E_{\text{pot}}(x, y) = 1.189 \times 10^3 \cdot \text{J}$

To get Valery's value:

$E_{\text{pot}}(x, y) - m_0 \cdot g \cdot (y_a + y_b) = 1.023 \times 10^3 \cdot \text{J}$

$E_{\text{pot}}(x, y) - m_0 \cdot g \cdot (y_a + y_b) = 104.274 \cdot \text{kgf} \cdot \text{m}$



Maximize for arch:

Initial values: $x_i := a + (i + 1) \cdot \frac{b - a}{N_S}$ $y_i := y_a + (i + 1) \cdot \frac{y_b - y_a}{N_S} + \frac{(x_i - a) \cdot (b - x_i)}{10 \cdot m}$

Vorgabe

Abschnitte(a, b, x, y) = 0

$\begin{pmatrix} x \\ y \end{pmatrix} := \text{Maximieren}(E_{\text{pot}}, x, y)$

ERR = 3.072×10^{-12}

TOL = 1×10^{-8}

CTOL = 1×10^{-9}

Abschnitte(a, b, x, y) =

	0	
0	0	
1	0	
2	0	
3	0	
4	$-1.221 \cdot 10^{-15}$	· m
5	$1.11 \cdot 10^{-15}$	
6	$-8.549 \cdot 10^{-15}$	
7	0	
8	$6.994 \cdot 10^{-15}$	
9	...	

$E_{\text{pot}}(x, y) = 2.312 \times 10^3 \cdot \text{J}$

To get Valery's value:

$E_{\text{pot}}(x, y) - m_0 \cdot g \cdot (y_a + y_b) = 2.145 \times 10^3 \cdot \text{J}$

$E_{\text{pot}}(x, y) - m_0 \cdot g \cdot (y_a + y_b) = 218.726 \cdot \text{kgf} \cdot \text{m}$

