

data:=READEXCEL(“.\part 2.xlsx”, “Sheet1!A6:B60”)=

a:=data<sup>(0)</sup>

λ:=data<sup>(1)</sup>

0.6664	261.1515
0.6675	292.8182
0.6874	261.7273
0.6886	292.2424
0.71	262.303
0.7112	291.6667
0.7342	262.8788
0.7356	291.0909
0.7603	263.4546
0.7617	290.5152
0.7882	264.0303
0.7898	289.9394
⋮	

a=

0.6664
0.6675
0.6874
0.6886
0.71
0.7112
0.7342
0.7356
0.7603
0.7617
0.7882
0.7898
⋮

λ=

261.1515
292.8182
261.7273
292.2424
262.303
291.6667
262.8788
291.0909
263.4546
290.5152
264.0303
289.9394
⋮

$$\omega := \frac{(2 \cdot \pi \cdot 3 \cdot 10^{17})}{\lambda}$$

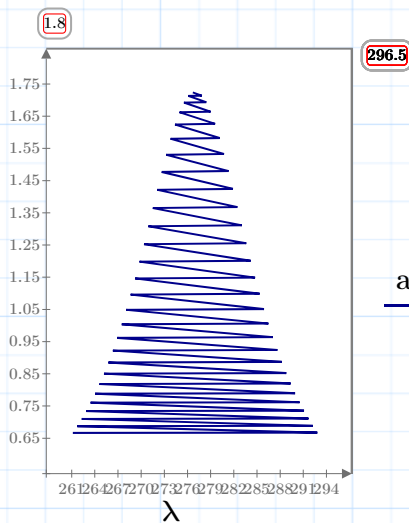
$$\lambda_1 := \frac{(2 \cdot \pi \cdot 3 \cdot 10^{17})}{\omega}$$

$$\alpha := a \cdot \frac{(2.303)}{1.88 \cdot 10^{-7}}$$

min(a)=0.6664

max(a)=1.7238

i:=1..rows(a)



a

→  
ω =

7.22 · 10 <sup>15</sup>
6.44 · 10 <sup>15</sup>
7.2 · 10 <sup>15</sup>
6.45 · 10 <sup>15</sup>
7.19 · 10 <sup>15</sup>
6.46 · 10 <sup>15</sup>
7.17 · 10 <sup>15</sup>
6.48 · 10 <sup>15</sup>
7.15 · 10 <sup>15</sup>
6.49 · 10 <sup>15</sup>
7.14 · 10 <sup>15</sup>
6.5 · 10 <sup>15</sup>
⋮

→  
α =

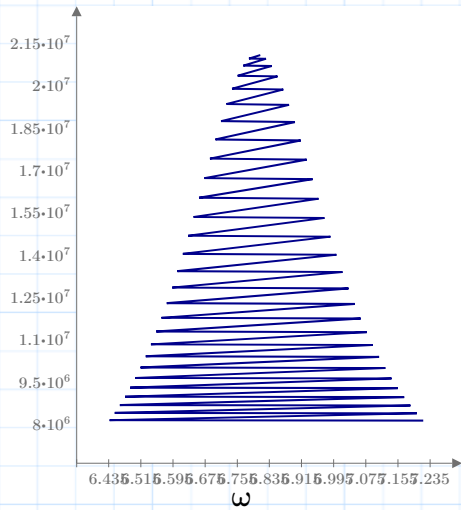
8.1634 · 10 <sup>6</sup>
8.1765 · 10 <sup>6</sup>
8.4209 · 10 <sup>6</sup>
8.4349 · 10 <sup>6</sup>
8.6973 · 10 <sup>6</sup>
8.7124 · 10 <sup>6</sup>
8.9943 · 10 <sup>6</sup>
9.0105 · 10 <sup>6</sup>
9.3133 · 10 <sup>6</sup>
9.3307 · 10 <sup>6</sup>
9.6559 · 10 <sup>6</sup>
9.6747 · 10 <sup>6</sup>
⋮

max(ω)=7.2179 · 10<sup>15</sup>

min(ω)=6.4373 · 10<sup>15</sup>

max(α)=2.1117 · 10<sup>7</sup>

min(α)=8.1634 · 10<sup>6</sup>



$$x := \text{cspline}(\alpha, \omega)$$

$$r1 := \max(\omega) - 0.0135 \cdot 10^{15}$$

$$r2 := \min(\omega) + 0.0135 \cdot 10^{15}$$

$$r1 = 7.2044 \cdot 10^{15}$$

$$r2 = 6.4508 \cdot 10^{15}$$

$\alpha$

$$\omega1 := r2, (r2 + (0.0135 \cdot 10^{15})) \dots r1$$

$$\omega1 = \begin{bmatrix} 6.4508 \cdot 10^{15} \\ 6.4643 \cdot 10^{15} \\ 6.4778 \cdot 10^{15} \\ 6.4913 \cdot 10^{15} \\ 6.5048 \cdot 10^{15} \\ 6.5183 \cdot 10^{15} \\ 6.5318 \cdot 10^{15} \\ 6.5453 \cdot 10^{15} \\ 6.5588 \cdot 10^{15} \\ 6.5723 \cdot 10^{15} \\ 6.5858 \cdot 10^{15} \\ 6.5993 \cdot 10^{15} \\ \vdots \end{bmatrix}$$

$\vec{\lambda1} =$

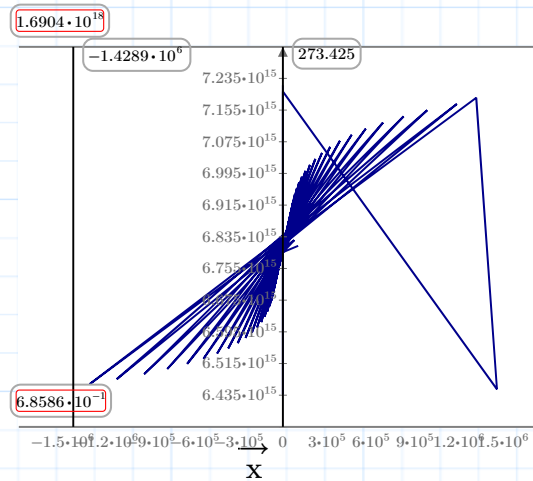
$$\begin{bmatrix} 261.1515 \\ 292.8182 \\ 261.7273 \\ 292.2424 \\ 262.303 \\ 291.6667 \\ 262.8788 \\ 291.0909 \\ 263.4546 \\ 290.5152 \\ 264.0303 \\ 289.9394 \\ \vdots \end{bmatrix}$$

$\vec{x} =$

$$\begin{bmatrix} 0 \\ 3 \\ 2 \\ 1.46 \cdot 10^6 \\ 1.32 \cdot 10^6 \\ -1.32 \cdot 10^6 \\ 1.19 \cdot 10^6 \\ -1.13 \cdot 10^6 \\ 9.84 \cdot 10^5 \\ -9.45 \cdot 10^5 \\ 8.23 \cdot 10^5 \\ -7.88 \cdot 10^5 \\ \vdots \end{bmatrix}$$

$\vec{\omega} =$

$$\begin{bmatrix} 7.2179 \cdot 10^{15} \\ 6.4373 \cdot 10^{15} \\ 7.202 \cdot 10^{15} \\ 6.45 \cdot 10^{15} \\ 7.1862 \cdot 10^{15} \\ 6.4627 \cdot 10^{15} \\ 7.1704 \cdot 10^{15} \\ 6.4755 \cdot 10^{15} \\ 7.1548 \cdot 10^{15} \\ 6.4883 \cdot 10^{15} \\ 7.1392 \cdot 10^{15} \\ 6.5012 \cdot 10^{15} \\ \vdots \end{bmatrix}$$



$\vec{\omega}$

$$\Delta\alpha(\alpha1) := \text{interp}(x, \alpha, \omega, \alpha1)$$

$$\alpha1 := \text{submatrix}(\alpha, 0, 20, 0, 0)$$

$$\overrightarrow{\alpha1} = \begin{bmatrix} 8.1634 \cdot 10^6 \\ 8.1765 \cdot 10^6 \\ 8.4209 \cdot 10^6 \\ 8.4349 \cdot 10^6 \\ 8.6973 \cdot 10^6 \\ 8.7124 \cdot 10^6 \\ 8.9943 \cdot 10^6 \\ 9.0105 \cdot 10^6 \\ 9.3133 \cdot 10^6 \\ 9.3307 \cdot 10^6 \\ 9.6559 \cdot 10^6 \\ 9.6747 \cdot 10^6 \\ \vdots \end{bmatrix} \quad \overrightarrow{\Delta\alpha(\alpha)} = \begin{bmatrix} \vdots \\ 6.4883 \cdot 10^{15} \\ 7.1392 \cdot 10^{15} \\ 6.5012 \cdot 10^{15} \\ 7.1236 \cdot 10^{15} \\ 6.5141 \cdot 10^{15} \\ 7.1082 \cdot 10^{15} \\ 6.5271 \cdot 10^{15} \\ 7.0928 \cdot 10^{15} \\ 6.5402 \cdot 10^{15} \\ 7.0774 \cdot 10^{15} \\ 6.5533 \cdot 10^{15} \\ 7.0622 \cdot 10^{15} \\ \vdots \end{bmatrix}$$

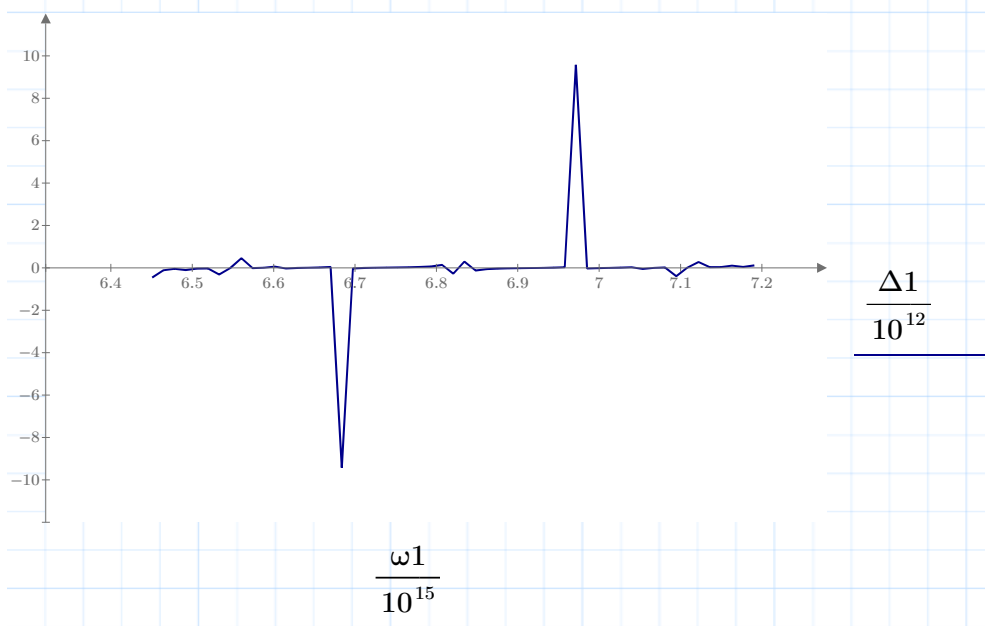
$$\Delta n(\omega1) := \left( \left[ 3 \cdot \frac{10^{10}}{\pi} \right] \right) \left[ \int_{r2}^{\overrightarrow{\omega1} + 0.0135 \cdot 10^{15}} \left( \frac{\overrightarrow{\Delta\alpha(\alpha1)}}{\overrightarrow{\omega}^2 - \overrightarrow{\omega1}^2} \right) d\omega + \int_{\overrightarrow{\omega1} - 0.0135 \cdot 10^{15}}^{r1} \left( \frac{\overrightarrow{\Delta\alpha(\alpha1)}}{\overrightarrow{\omega}^2 - \overrightarrow{\omega1}^2} \right) d\omega \right]$$

$$\overrightarrow{\Delta n(\omega1)} = ?$$

$$i := 0 \dots \text{last}(\alpha) \quad \omega1_i := r2 + i \cdot \frac{r1 - r2}{\text{rows}(\alpha)}$$

$$\Delta n(\omega1) := 3 \cdot \frac{10^{10}}{\pi} \left( \int_{r2}^{\omega1 + 0.0135 \cdot 10^{15}} \frac{1}{\omega^2 - \omega1^2} d\omega + \int_{\omega1 - 0.0135 \cdot 10^{15}}^{r1} \frac{1}{\omega^2 - \omega1^2} d\omega \right)$$

$$\Delta1 := \overrightarrow{\Delta n(\omega1) \cdot \Delta \alpha(\alpha)} = \begin{bmatrix} -4.6178 \cdot 10^{11} \\ -1.1882 \cdot 10^{11} \\ -4.8841 \cdot 10^{10} \\ -1.0652 \cdot 10^{11} \\ -3.9079 \cdot 10^{10} \\ -3.1557 \cdot 10^{10} \\ \vdots \end{bmatrix} \quad \omega1 = \begin{bmatrix} 6.4508 \cdot 10^{15} \\ 6.4645 \cdot 10^{15} \\ 6.4782 \cdot 10^{15} \\ 6.4919 \cdot 10^{15} \\ 6.5056 \cdot 10^{15} \\ 6.5193 \cdot 10^{15} \\ \vdots \end{bmatrix}$$

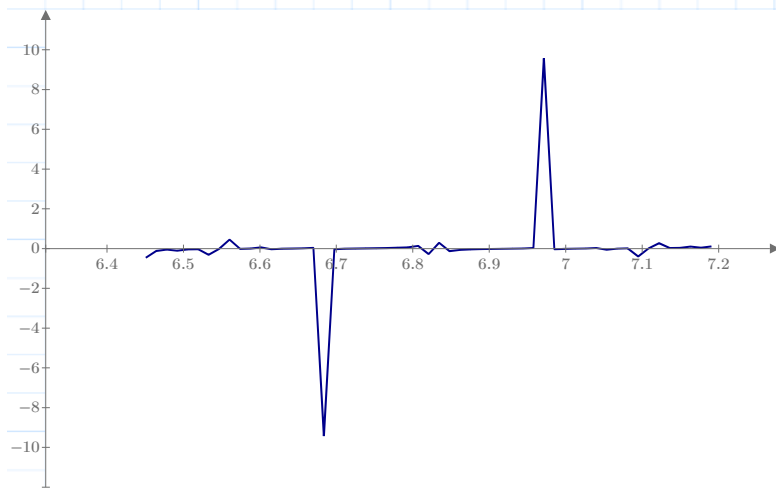


But it looks like you don't need your interpolation function at all because you only use it for the elements of  $\alpha$ , so  $\Delta \alpha(\alpha)$  will always return the corresponding element of  $\omega$ . See below

$$i:=0..\text{last}(\alpha) \qquad \omega1_i:=r2+i\cdot\frac{r1-r2}{\text{rows}(\alpha)}$$

$$\Delta n(\omega1):=3\cdot\frac{10^{10}}{\pi}\left(\int\limits_{r2}^{\omega1+0.0135\cdot10^{15}}\frac{1}{\omega^2-\omega1^2}d\omega+\int\limits_{\omega1-0.0135\cdot10^{15}}^{r1}\frac{1}{\omega^2-\omega1^2}d\omega\right) \qquad \Delta2:=\overrightarrow{\Delta n(\omega1)}\cdot\omega=$$

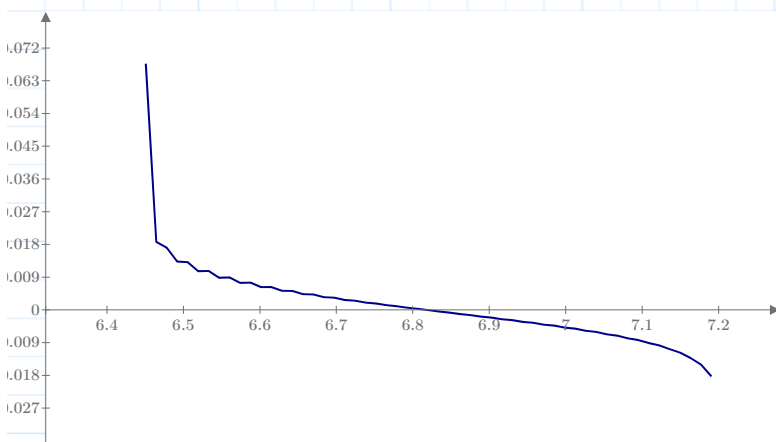
$$\begin{bmatrix} -4.6178\cdot10^{11} \\ -1.1882\cdot10^{11} \\ -4.8841\cdot10^{10} \\ -1.0652\cdot10^{11} \\ -3.9079\cdot10^{10} \\ -3.1557\cdot10^{10} \\ \vdots \end{bmatrix}$$



$$\Delta2\cdot10^{-12}$$

$$\omega1\cdot10^{-15}$$

$$\Delta n(\omega1):=3\cdot\frac{10^{10}}{\pi}\left(\int\limits_{r2}^{\omega1-10^{13}}\frac{1}{\omega^2-\omega1^2}d\omega+\int\limits_{\omega1+10^{13}}^{r1}\frac{1}{\omega^2-\omega1^2}d\omega\right) \qquad \Delta3:=\overrightarrow{\Delta n(\omega1)}\cdot\omega=$$



$$\Delta3\cdot10^{-12}$$

$$\omega1\cdot10^{-15}$$