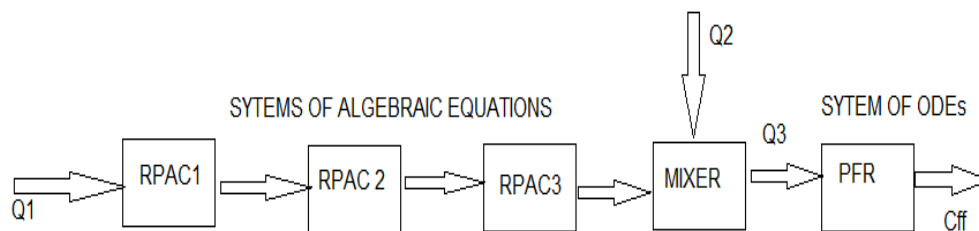


So my constraint in here its Q_1 which can vary from 20 to 200

I had to find what value of Q_1 in that interval gives the higher possible value of C_{ff} at the end of this problem (**concentrations of F at the final reactor**)

I have 3 RPACs (**systems of algebraic equations like example 2**), values found in one are used as initial values in the next one. the flow coming out of the third RPAC mix with a stream in a mixer resulting in the incoming conditions for the Final reactor (**system of diff equation like example 3**).

Look at the diagram in the right for better understanding



What happens between RPACs it is not important neither what happens in the mixer, but what's coming out of the PFR (**differential equation system**),

Changing Q_1 results in an augmentation of Q_3 since $Q_3 = Q_1 + Q_2$ (fixed)

How I did it?, I didn't know how to make it using Mathcad's function. so I proved values from 20 to 200, starting from 20 and increasing it by 5 till 200. I didn't have a good time :/.

Well I found **the higher value of C_{ff} by fixing $Q_1 = 35$ ($C_{ff} = 1.93$)**

how would you maximize the value of C_{ff} at the final reactor (system of ODEs) by changing Q_1 (in the beginning of the systems of algebraic equations)?

Conditions initiales

$C_{a0} := 8$	$k_1 := 0.01$	Varyng this variable subject to: Constraint:	$20 \leq Q_1 \leq 200$
$C_{b0} := 8$	$k_2 := 0.005$		
$C_{c0} := 0$	$k_3 := 0.02$		
$C_{d0} := 35$	$k_4 := 0.001$		

$Q_1 := 115$

Premier RPAC

Guess

$C_{a1} := 5$ $C_{b1} := 5$ $C_{c1} := 3$ $C_{d1} := 3$ $V_{r1} := 50$

Given

Bilans de matiere

$$\text{A: } Ca_0 = Ca_1 + k_1 \cdot Ca_1 \cdot Cb_1 \cdot \frac{Vr_1}{Q_1}$$

$$\text{B: } Cb_0 = Cb_1 - 0.5 \cdot k_2 \cdot Cc_1 \cdot \frac{Vr_1}{Q_1} + k_1 \cdot Ca_1 \cdot Cb_1 \cdot \frac{Vr_1}{Q_1}$$

$$\text{C: } Cc_0 = Cc_1 - k_1 \cdot Ca_1 \cdot Cb_1 \cdot \frac{Vr_1}{Q_1} + k_2 \cdot Cc_1 \cdot \frac{Vr_1}{Q_1}$$

$$\text{D: } Cd_0 = Cd_1 - k_2 \cdot Cc_1 \cdot \frac{Vr_1}{Q_1}$$

$$\begin{pmatrix} Ca_1 \\ Cb_1 \\ Cc_1 \\ Cd_1 \end{pmatrix} := \text{Find}(Ca_1, Cb_1, Cc_1, Cd_1)$$

Les Concentration a la sortie

$$Ca_1 = 7.74$$

$$Cb_1 = 7.74$$

$$Cc_1 = 0.26$$

$$Cd_1 = 35.001$$

Deuxieme RPAC

Guess

$$Ca_2 := 1 \quad Cb_2 := 1 \quad Cc_2 := 1 \quad Cd_2 := 1 \quad Vr_2 := 100$$

Given

Bilans de matieres

$$\text{A: } Ca_1 = Ca_2 + k_1 \cdot Ca_2 \cdot Cb_2 \cdot \frac{Vr_2}{Q_1}$$

$$\text{B: } Cb_1 = Cb_2 - 0.5 \cdot k_2 \cdot Cc_2 \cdot \frac{Vr_2}{Q_1} + k_1 \cdot Ca_2 \cdot Cb_2 \cdot \frac{Vr_2}{Q_1}$$

$$\text{C: } Cc_1 = Cc_2 - k_1 \cdot Ca_2 \cdot Cb_2 \cdot \frac{Vr_2}{Q_1} + k_2 \cdot Cc_2 \cdot \frac{Vr_2}{Q_1}$$

$$\text{D: } Cd_1 = Cd_2 - k_2 \cdot Cc_2 \cdot \frac{Vr_2}{Q_1}$$

$$\begin{pmatrix} Ca2 \\ Cb2 \\ Cc2 \\ Cd2 \end{pmatrix} := \text{Find}(Ca2, Cb2, Cc2, Cd2)$$

Les Concentration a la sortie

$$Ca2 = 7.279$$

$$Cb2 = 7.281$$

$$Cc2 = 0.718$$

$$Cd2 = 35.004$$

Troisieme RPAC

Guess

$$Ca3 := 0 \quad Cb3 := 0 \quad Cc3 := 0 \quad Cd3 := 0 \quad Vr3 := 500$$

Given

Bilans de matieres

$$\mathbf{A:} \quad Ca2 = Ca3 + k1 \cdot Ca3 \cdot Cb3 \cdot \frac{Vr3}{Q1}$$

$$\mathbf{B:} \quad Cb2 = Cb3 - 0.5 \cdot k2 \cdot Cc3 \cdot \frac{Vr3}{Q1} + k1 \cdot Ca3 \cdot Cb3 \cdot \frac{Vr3}{Q1}$$

$$\mathbf{C:} \quad Cc2 = Cc3 - k1 \cdot Ca3 \cdot Cb3 \cdot \frac{Vr3}{Q1} + k2 \cdot Cc3 \cdot \frac{Vr3}{Q1}$$

$$\mathbf{D:} \quad Cd2 = Cd3 - k2 \cdot Cc3 \cdot \frac{Vr3}{Q1}$$

$$\begin{pmatrix} Ca3 \\ Cb3 \\ Cc3 \\ Cd3 \end{pmatrix} := \text{Find}(Ca3, Cb3, Cc3, Cd3)$$

Les Concentration a la sortie

$$Ca3 = 5.807$$

$$Cb3 = 5.832$$

$$Cc3 = 2.143$$

$$Cd3 = 35.05$$

Unite de Melangeur

courrant d'entre

$$Q1 = 115$$

$$Q2 := 30$$

Courrant sortant des RPAC

$$\begin{aligned}Ca_3 &= 5.807 \\Cb_2 &= 7.281 \\Cc_3 &= 2.143 \\Cd_3 &= 35.05\end{aligned}$$

Courrant de produit E

$$Ce := 10$$

Bilan de matiere

Q3 DEPENDS OF Q1, Q2 IS FIXED

$$Q_3 := Q_1 + Q_2$$

$$Ca_3 \cdot Q_1 = Ca_4 \cdot Q_3$$

$$Cb_3 \cdot Q_1 = Cb_4 \cdot Q_3$$

$$Cc_3 \cdot Q_1 = Cc_4 \cdot Q_3$$

$$Cd_3 \cdot Q_1 = Cd_4 \cdot Q_3$$

$$Ce \cdot Q_2 = Ce_4 \cdot Q_3$$

$$Ca_4 := \frac{Ca_3 \cdot Q_1}{Q_3}$$

$$Cd_4 := \frac{Cd_3 \cdot Q_1}{Q_3}$$

$$Cb_4 := \frac{Cb_3 \cdot Q_1}{Q_3}$$

$$Ce_4 := \frac{Ce \cdot Q_2}{Q_3}$$

$$Cc_4 := \frac{Cc_3 \cdot Q_1}{Q_3}$$



Courrant de sortie

$$Q_3 = 145$$

$$Ca_4 = 4.605 \quad Cd_4 = 27.799$$

$$Cb_4 = 4.625 \quad Ce_4 = 2.069$$

$$Cc_4 = 1.7$$

Reacteur Tubulaire

Concentrations d'entre

$$Ca_4 = 4.605 \quad Ce_4 = 2.069$$

$$Cb_4 = 4.625 \quad Cf_4 := 0$$

$$Cc_4 = 1.7 \quad Cg_4 := 0$$

$$Cd_4 = 27.799$$

Given

Bilans de matiere

$$A: \quad \frac{d}{d\tau} Ca(\tau) = -k_1 \cdot Ca(\tau) \cdot Cb(\tau)$$

$$B: \frac{d}{d\tau} C_b(\tau) = -k_1 \cdot C_a(\tau) \cdot C_b(\tau) + 0.5 \cdot k_2 \cdot C_c(\tau)$$

$$C: \frac{d}{d\tau} C_c(\tau) = k_1 \cdot C_a(\tau) \cdot C_b(\tau) - k_2 \cdot C_c(\tau) - k_3 \cdot C_c(\tau) \cdot C_e(\tau)$$

$$D: \frac{d}{d\tau} C_d(\tau) = k_2 \cdot C_c(\tau) + k_3 \cdot C_c(\tau) \cdot C_e(\tau) - k_4 \cdot C_f(\tau) \cdot (C_b(\tau) \cdot C_d(\tau))^{0.5}$$

$$E: \frac{d}{d\tau} C_e(\tau) = -k_3 \cdot C_c(\tau) \cdot C_e(\tau)$$

$$F: \frac{d}{d\tau} C_g(\tau) = k_4 \cdot C_f(\tau) \cdot (C_b(\tau) \cdot C_d(\tau))^{0.5}$$

$$G: \frac{d}{d\tau} C_f(\tau) = k_3 \cdot C_c(\tau) \cdot C_e(\tau) - k_4 \cdot C_f(\tau) \cdot (C_b(\tau) \cdot C_d(\tau))^{0.5}$$

$$C_a(0) = C_{a4} \quad C_b(0) = C_{b4} \quad C_c(0) = C_{c4} \quad C_d(0) = C_{d4}$$

$$C_e(0) = C_{e4} \quad C_f(0) = C_{f4} \quad C_g(0) = C_{g4}$$

$$\begin{pmatrix} C_{af} \\ C_{bf} \\ C_{cf} \\ C_{df} \\ C_{ef} \\ C_{ff} \\ C_{gf} \end{pmatrix} := \text{Odesolve} \left[\begin{pmatrix} C_a \\ C_b \\ C_c \\ C_d \\ C_e \\ C_f \\ C_g \end{pmatrix}, \tau, 300 \right]$$

Reacteur V= 2000

Concentrations a la sortie

$$V_{r1} := 2000 \quad \tau_1 := \frac{V_{r1}}{Q_3}$$

As you can see the variable τ_1 (TAU) only depends on Q_3 since V_{r1} is fixed. and Q_3 depends on Q_1 .

$$\tau_1 = 13.793$$

$$C_{af}(\tau_1) = 2.798$$

$$C_{bf}(\tau_1) = 2.893$$

$$C_{cf}(\tau_1) = 2.42$$

$$C_{df}(\tau_1) = 28.823$$

$$C_{ef}(\tau_1) = 1.132$$

$$C_{ff}(\tau_1) = 0.874$$

I WANT TO FIND THE MAXIMUM VALUE OF C_{ff} CHANGING Q_1

$$C_{gf}(\tau_1) = 0.063$$

